

Analysis III for Engineering Students

Work Sheet 4

Exercise 1:

Compute the Taylor polynomial of second degree for the function

$$f(x, y) = (y + \cos y) \sin x$$

about the point $(x_0, y_0) = \left(\frac{\pi}{2}, 0\right)$ and provide the upper bound for the error of approximation of f by T_2 at point $(x, y) = (0, 0)$.

Exercise 2:

Compute and classify all stationary points of the following functions

a) $f(x, y) = \frac{3x^2}{2} + x^3 - y^3 + 3y,$

b) $f(x, y) = 2(x^2 + y^2)^2 - x^2 - y^2,$

c) $f(x, y) = \sqrt{x^2 + y^2},$

d) $f(x, y) = x \sin y.$

Discussion: 4.12. - 8.12.2023