# Analysis III for Engineering Students <br> <br> Homework sheet 3 

 <br> <br> Homework sheet 3}

## Exercise 1:

Compute the derivative in direction $\boldsymbol{h}=\left(h_{1}, h_{2}\right)^{T}$ for the function $f: \mathbb{R}^{2} \rightarrow \mathbb{R}$ $f(x, y)=x^{2}+y$ at the point $\left(x_{0}, y_{0}\right)$. What is the slope of the function at the point $(2,-3)$ in the directions given by the straight line $2 x+7 y=3$ ?

## Exercise 2:

Given the coordinate transformation

$$
\boldsymbol{\Phi}(r, \varphi)=\binom{x(r, \varphi)}{y(r, \varphi)}=\binom{2 r \cos \varphi}{3 r \sin \varphi}
$$

with $(r, \varphi) \in Q:=] 0,1] \times]-\frac{\pi}{2}, \frac{\pi}{2}[$.
a) Compute $\boldsymbol{J} \boldsymbol{\Phi}(r, \varphi)$ and $\operatorname{det}(\boldsymbol{J} \boldsymbol{\Phi}(r, \varphi))$ as well as
b) $\boldsymbol{\Phi}^{-1}(x, y), \boldsymbol{J} \boldsymbol{\Phi}^{-1}(x, y)$ and $\operatorname{det}\left(\boldsymbol{J} \boldsymbol{\Phi}^{-1}(x, y)\right)$.
c) Make a sketch of $Q$ and $\boldsymbol{\Phi}(Q)$.

