

# Approaching the Logic of Conversational Implicatures

Robert van Rooij & Katrin Schulz  
ILLC/University of Amsterdam  
R.A.M.vanRooij/K.Schulz@uva.nl

# 1. Introduction

## 1.1 Aim of the Research

⇒ Describe the logic of conversational implicatures (Grice '57)  
(particularly Quantity1-implicatures)

- formally precise account
- descriptive adequate
- explanatory convincing

⇒ formalize Grice's theory of conversational implicatures

# 1. Introduction

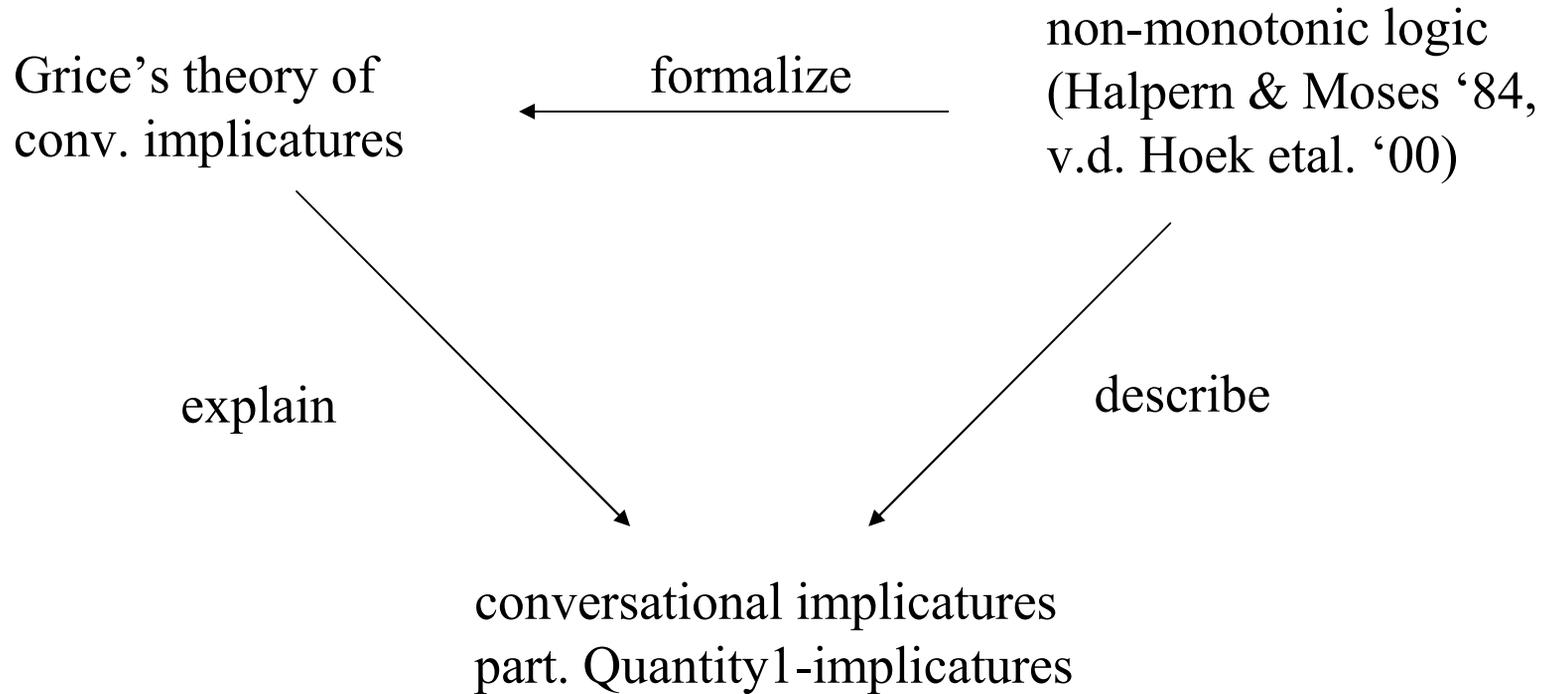
## 1.2 Motivation

⇒ The dilemma of pragmatics:

- conversational implicatures and Grice's theory thereof have become an enormous popular ingredient of semantic theories
- there exists no precise formulation of Grice's theory that is overall convincing

# 1. Introduction

## 1.3 The Strategy



# 1. Introduction

## 1.4 The Problem

- few available data
- which are theoretical preloaded
- and inconsistent with each other

⇒ We need serious data studies! Semantics has to grow up!

# 1. Introduction

## 1.5 Outline of the talk

1. Introduction
2. The Data
3. The Proposal
4. Critical Predictions
5. Conclusion

## 2. The Data

Paul: Who passed the examination?

Paula: Ann or Bob passed.

- scalar implicatures: *Not both, Ann and Bob passed.*
- exhaustive interpretation: *Nobody else passed.*
- clausal implicatures: *Paula doesn't know that Ann passed.*
- context dependence:

Paul: Did Ann or Bob pass the examination?

Paula: Yes, Ann or Bob passed.

### 3. The Proposal

#### 3.1 Formalizing Grice

Quantity1: The speaker makes the strongest relevant claim she can  
(Quality: given her knowledge)

⇒ Pragmatic interpretation function  $f: L \times C \longrightarrow p(S)$

Requirements on  $f(A,c)$ :

1. Speaker knows  $A$
2.  $A$  is a *strongest* claim the speaker could have made (given her knowledge)
3.  $A$  is a strongest claim with respect to what is *relevant*

## 3. The Proposal

### 3.1 Formalizing Grice

How to formalize the requirements?

#### 1. Speaker knows A

$$f(A,c) \models \mathbf{K}_s A$$

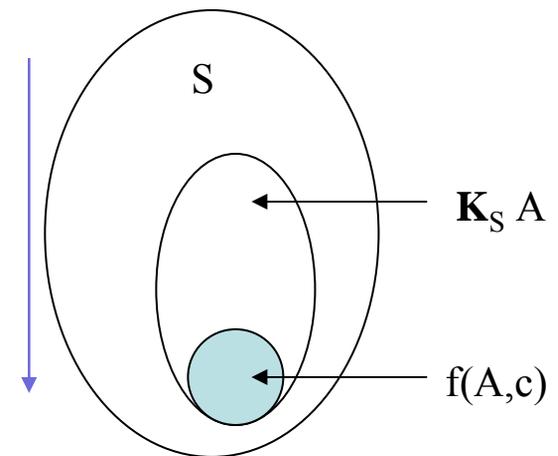
## 3. The Proposal

### 3.1 Formalizing Grice

How to formalize the requirements?

2.  $A$  is a *strongest* claim the speaker could have made (given her knowledge)

- impose an order  $\leq$  on  $\mathbf{S}$
- select minimal elements with respect to  $\leq$



## 3. The Proposal

### 3.1 Formalizing Grice

How to formalize the requirements?

3. A is maximal informative with respect to what is *relevant*

- relevant = helps to resolve the question  
→ speaker knows not more about the answer than she said with A

Paul: Who passed the examination?

Paula: Ann passed. →  $\neg \mathbf{K}_S P(\text{Bob})$

## 3. The Proposal

### 3.1 Formalizing Grice

Definition 1 (order):

$$\forall s_1, s_2 \in \mathbf{S}: s_1 \leq_P^1 s_2 \Leftrightarrow_{\text{def}} \forall v_2 \in R_2[w_2] \exists v_1 \in R_1[w_1]: P(v_1) \subseteq P(v_2)$$

Definition 2 (pragmatic interpretation function):

$$\text{eps}_1^S(A, P) = \{ s \in \mathbf{S} \mid s \models \mathbf{K}_S A \ \& \ \forall s' \in \mathbf{S} : s' \models \mathbf{K}_S A \Rightarrow s \leq_P^1 s' \}$$

### 3. The Proposal

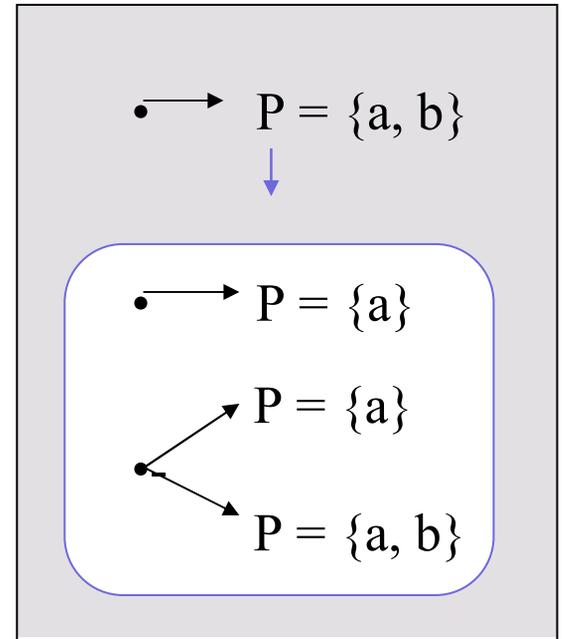
#### 3.2 Example

Paul: Who passed the examination?

Paula: Ann passed.

$$\text{eps}_1^S(P(a), P) \models \neg \mathbf{K}_S P(b)$$

$$\not\models \neg P(b)$$



## 3. The Proposal

### 3.3 Formalizing Competence

#### 3.3.1 The Simple Approach - does not work!

- Let  $C \subseteq S$  be the worlds where the speaker is competent.  
Then  $\text{eps}_1^C(A, P) = \text{scalar implicatures}$ .

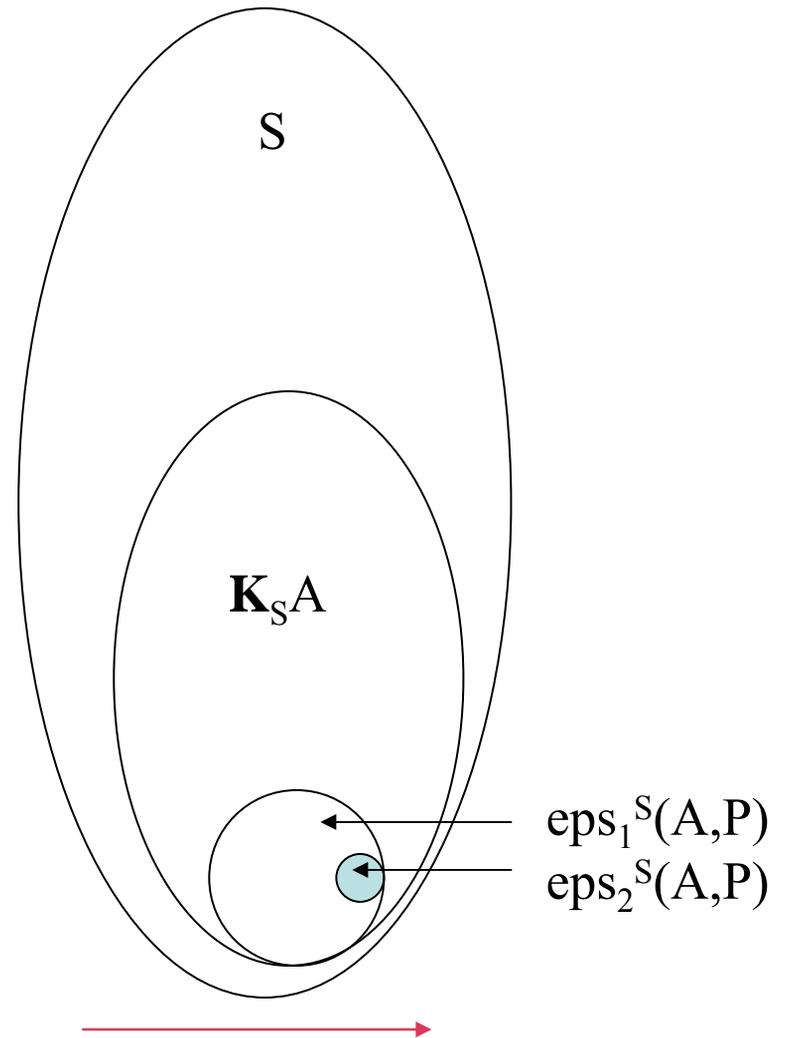


# 3. The Proposal

## 3.3 Formalizing Competence

### 3.3.2 Maximize Competence

- impose a second order  $\leq^2$  on S
- select among those worlds in  $\text{eps}_1^S$  those worlds where the speaker is maximal competent



## 3. The Proposal

### 3.3 Formalizing Competence

Definition 2 (order):

$$\forall s_1, s_2 \in S: s_1 \leq_P^2 s_2 \Leftrightarrow_{\text{def}} \forall v_1 \in R_1[w_1] \exists v_2 \in R_2[w_2]: P(v_1) \subseteq P(v_2)$$

Definition 4 (pragmatic interpretation function):

$$\text{eps}_2^S(A, c) = \{ s \in \text{eps}_1^S(A, c) \mid \neg \exists s' \in \text{eps}_1^S(A, c): s' <_P^2 s \}$$

### 3. The Proposal

#### 3.4 Example

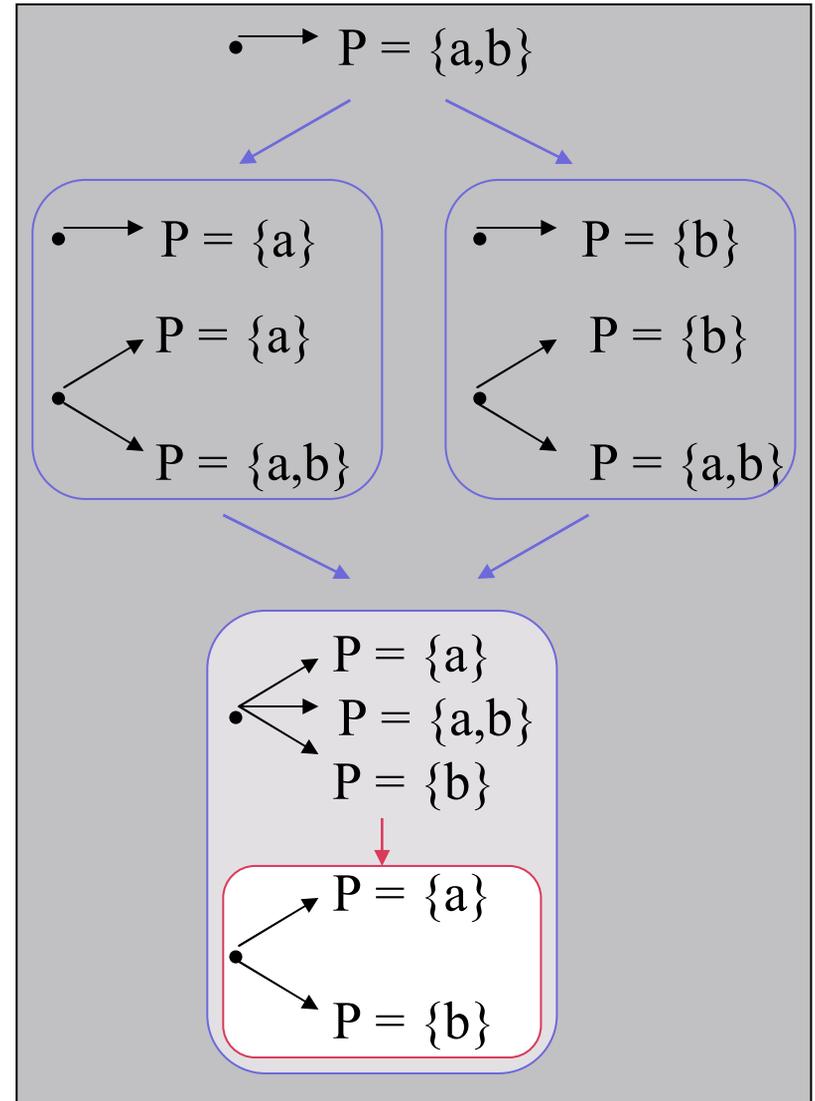
Paul: Who passed the examination?

Paula: Ann or Bob passed.

$$\text{eps}_2^S(P(a) \vee P(b), P)$$

$$\models \neg (P(a) \wedge P(b))$$

$$\models \neg \mathbf{K}_S \neg P(a) \wedge \neg \mathbf{K}_S \neg P(b)$$



## 4. Critical Predictions

### 4.1 Context-dependence

- ? Do answers always come with the inferences we predict?
- ? Do Quantity1-implicatures occur also in other contexts than answers to overt questions?

## 4. Critical Predictions

### 4.1 How convincing are the orders?

- The Gricean order  $\leq^1$

Paul: Who passed the examination?

Paula: Ann passed.

$\rightarrow \neg \mathbf{K}_S P(\text{Bob})$   
 $\nearrow \neg \mathbf{K}_S \neg P(\text{Bob})$

? In the context of questions, do interpreters also infer incompetence of the speaker with respect to the complement of the question predicate?

## 4. Critical Predictions

### 4.3 The Functionality Problem

Paul: Who passed the examination?

Paula: (i) Not Ann.

(ii) If he did not oversleep Bob passed.

(iii) Maybe Ann passed.

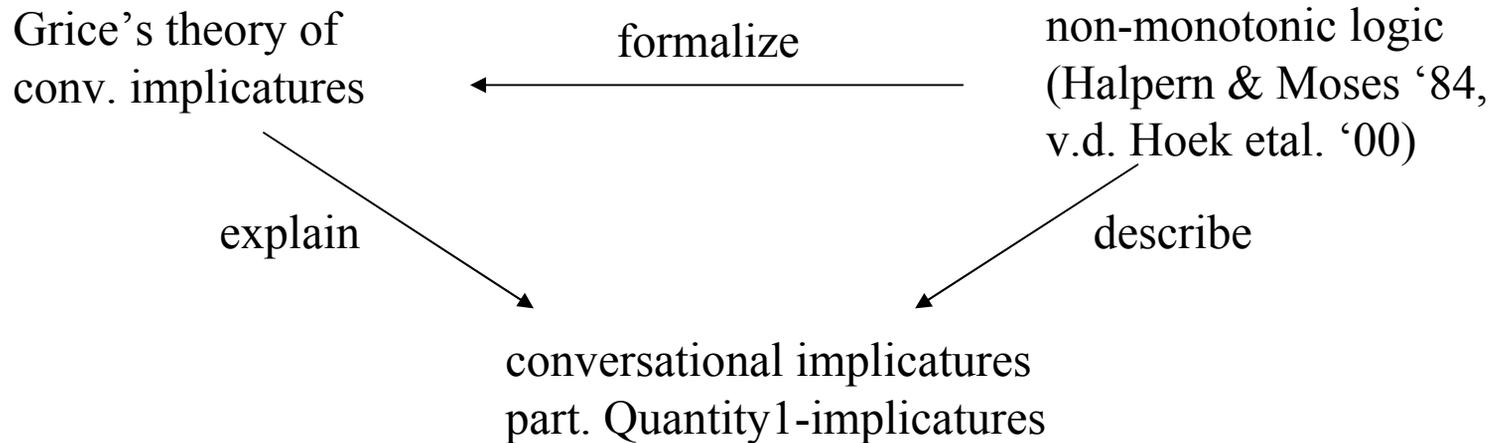
...

? What form-aspects are relevant for Quantity1-implicatures?

? Can we give a Gricean-like motivation for such form restrictions?

## 5. Conclusions

### 5.1 The Approach



- two pragmatic interpretation functions
  1.  $\text{eps}_1^S \rightarrow$  formalizes inferences due to Quantity1 and Quality
  2.  $\text{eps}_2^S \rightarrow$  formalizes maximizing competence

## 5. Conclusions

### 5.1 Achievements

- formally precise approach to conversational implicatures; hence, strong in its predictions
- unified account to Quantity<sup>1</sup>-implicatures
- based on the well-known and well-established ideas of Grice

### 5.2 Open Questions

- test the descriptive adequacy of the approach
- the role of competence in natural language interpretation
- extension to other conversational implicatures