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Ano III

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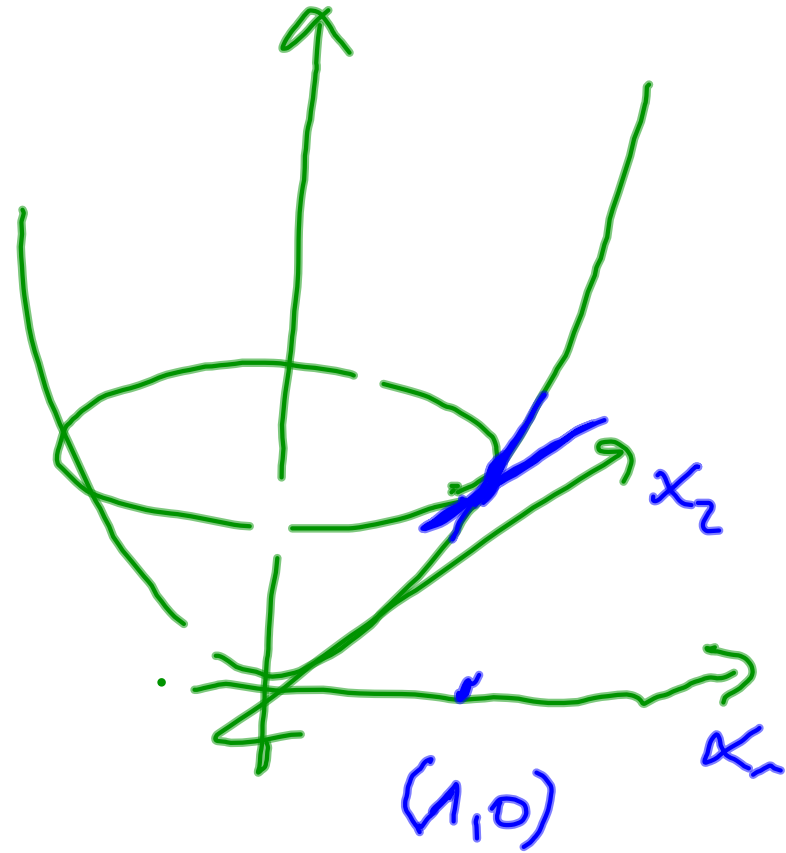
$$\frac{\partial f}{\partial x_1} = \frac{\partial}{\partial x_1} (x_1^2 + x_2^2) =$$

$$= 2x_1$$

$$\frac{\partial f}{\partial x_2} = 2x_2$$

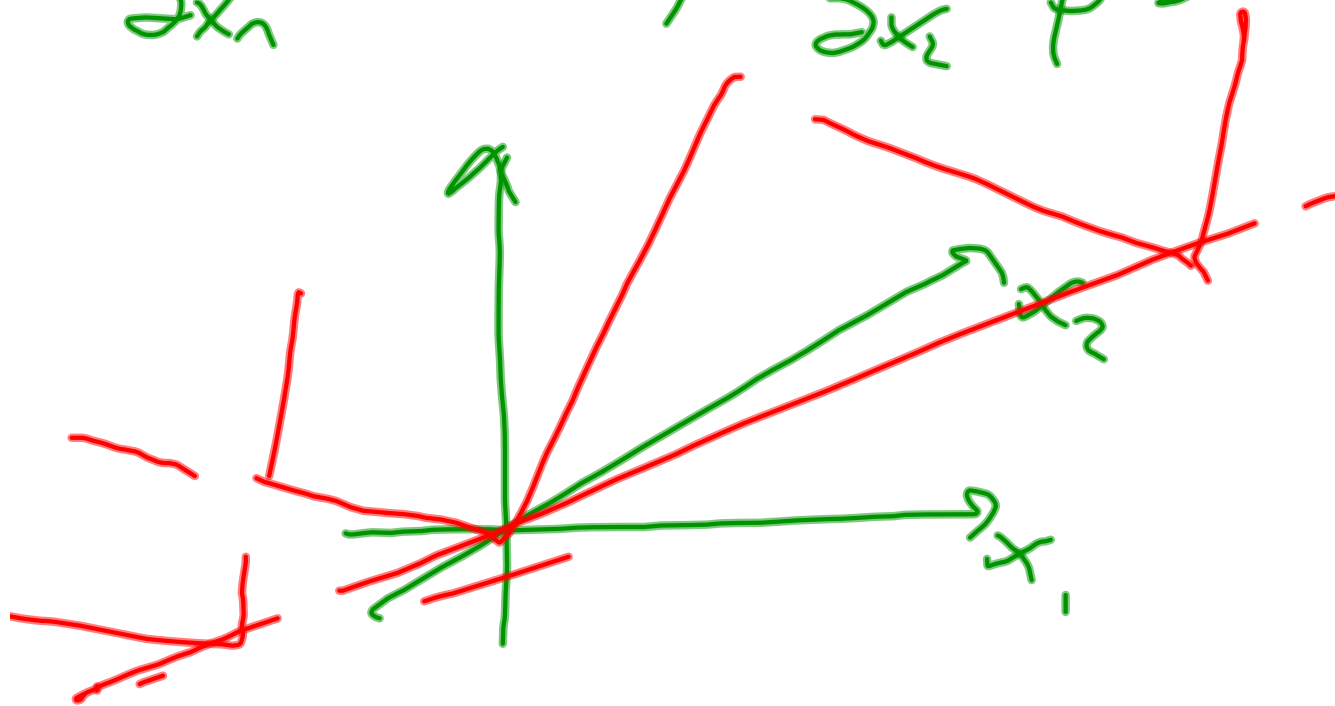
$$\frac{\partial f}{\partial x_1} (1,0) = 1$$

$$\frac{\partial f}{\partial x_2} (1,0) = 0$$

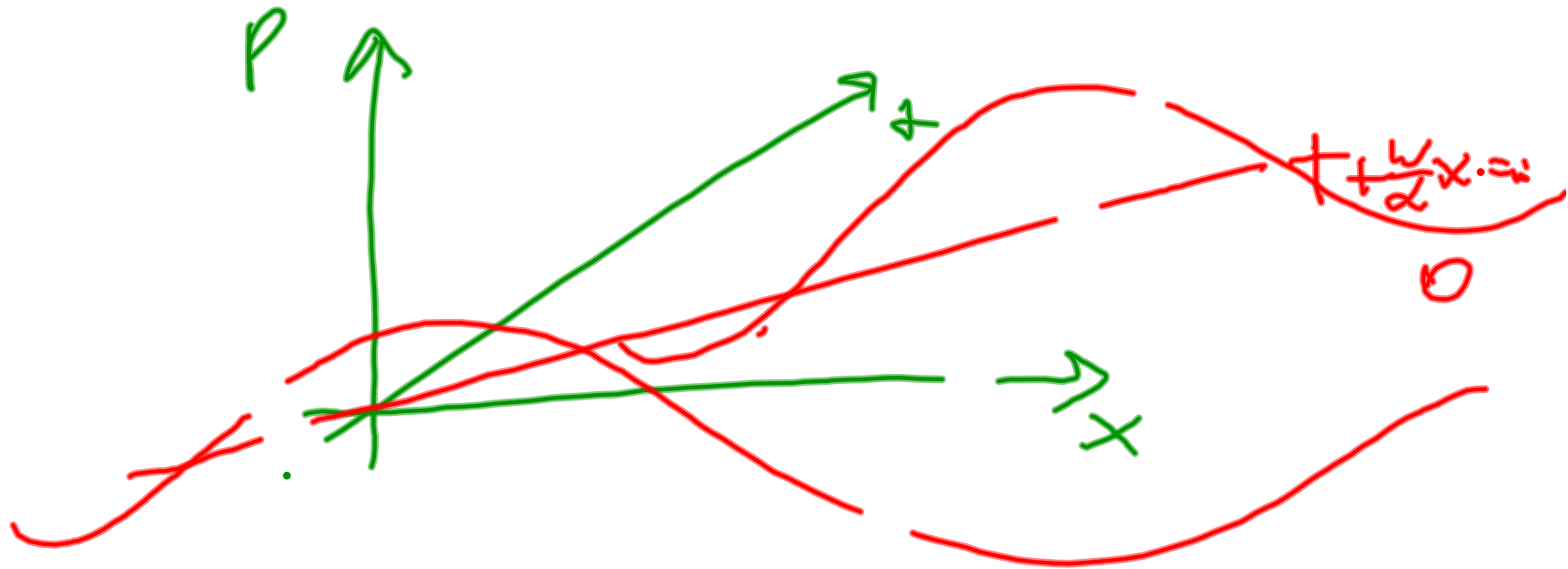


$$f(x_1, x_2) = x_2 + |x_2|$$

$$\frac{\partial f}{\partial x_1} = 1, \quad \frac{\partial f}{\partial x_2} \text{ ist bei } x_2 := 0$$



$$p(x, t) = A \sin(\alpha t + \omega x)$$
$$= A \sin\left(\alpha \left(t + \frac{\omega}{\alpha} x\right)\right)$$

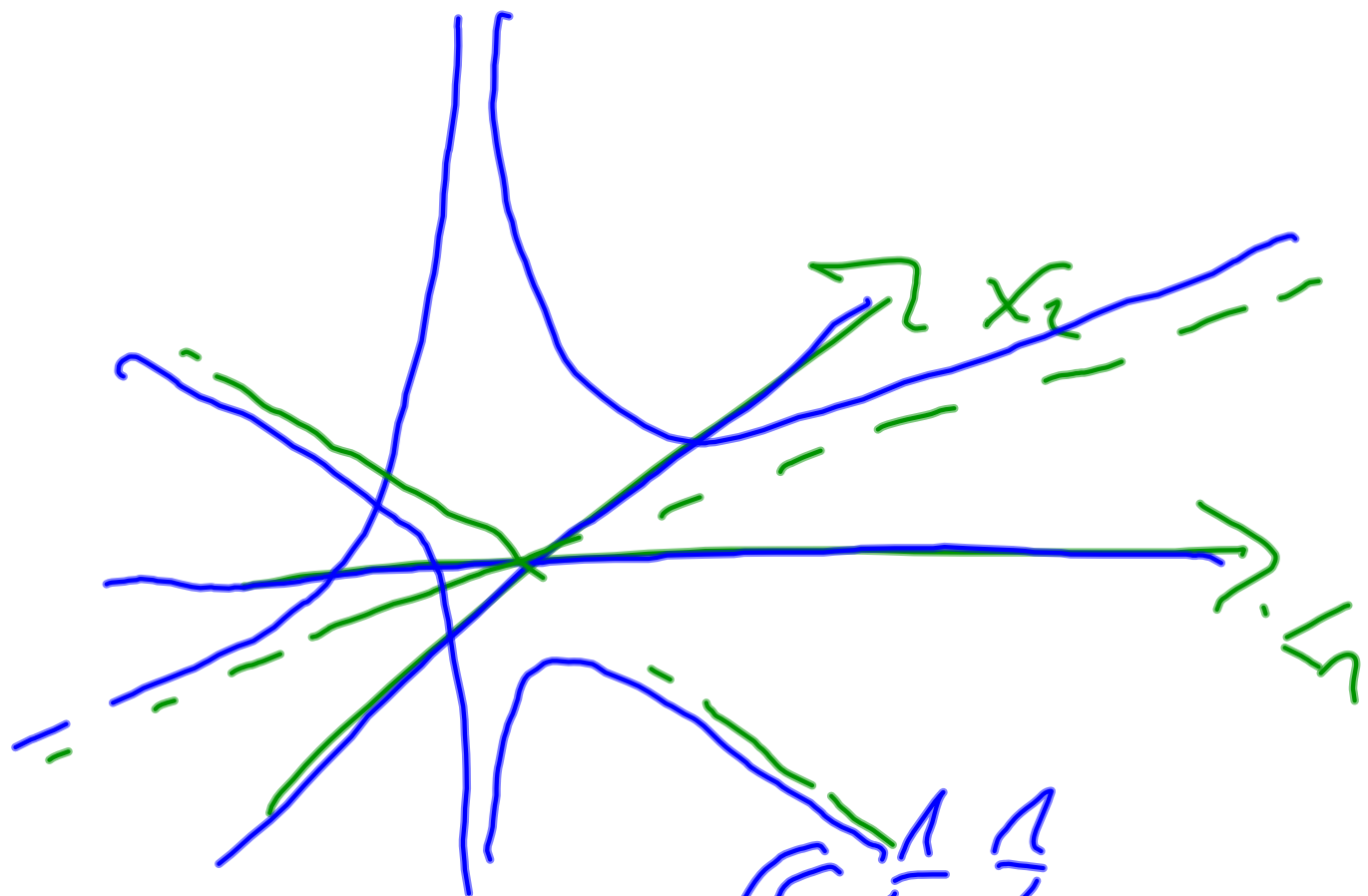


$$r(x) = \|x\|_2 = \sqrt{x_1^2 + x_2^2 + \dots + x_n^2}$$

$$\frac{\partial r}{\partial x_i} = \frac{2x_i}{2\sqrt{\dots}} = \frac{x_i}{r(x)}$$

$$\nabla r = \frac{1}{r(x)} \begin{pmatrix} x_1 \\ \vdots \\ x_n \end{pmatrix} = \frac{x}{r(x)}$$

$$f(x, y) = \begin{cases} \frac{xy}{(x^2 + y^2)^2} \\ 0 \end{cases} \quad \text{at } (0, 0)$$



$x \Rightarrow$

$$f(x, x) = \frac{x^2}{2x^2}$$

$$\frac{1}{4} x^2$$

$$\frac{1}{4} x^2$$

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$$\begin{aligned}
f(x) - f(x_0) &= f(x_1, x_2) - f(x_1^0, x_2^0) = \\
&= f(x_1, x_2) - f(x_1, x_2^0) \\
&\quad + f(x_1, x_2^0) - f(x_1^0, x_2^0) \quad \text{in.} \\
&= \frac{\partial f}{\partial x_2}(x_1, \xi_2) (x_2 - x_2^0) \\
&\quad + \frac{\partial f}{\partial x_1}(\xi_1, x_2^0) (x_1 - x_1^0)
\end{aligned}$$

$x \rightarrow x^0$
 $\left\{ \begin{array}{l} x_2 \rightarrow x_2^0 \\ x_1 \rightarrow x_1^0 \end{array} \right.$

$$|f(x) - f(x_0)| \leq C_1 |x_2 - x_2^0| + C_2 |x_1 - x_1^0| \rightarrow 0$$

$$f = f(x, y)$$

$$\frac{\partial^2}{\partial x \partial y} f = \frac{\partial}{\partial x} \left(\frac{\partial f}{\partial y} \right) \stackrel{?}{=} \frac{\partial}{\partial y} \left(\frac{\partial f}{\partial x} \right) = \frac{\partial^2}{\partial y \partial x} f$$

$$f = 2x_1$$

$$\frac{\partial^2}{\partial x_1 \partial x_2} f = 0 = \frac{\partial^2}{\partial x_2 \partial x_1} f$$

$$\frac{\partial f}{\partial x}(0,0) = \lim_{t \rightarrow 0} \frac{f(t,0) - f(0,0)}{t} = \lim_{t \rightarrow 0} \frac{t \cdot 0 - 0}{t} = 0$$

$$\frac{\partial f}{\partial x}(x,y) = y \frac{x^2 - y^2}{x^2 + y^2} + xy \frac{2x(x^2 + y^2) - 2x(x^2 - y^2)}{(x^2 + y^2)^2} = 0$$

$$\frac{\partial^2 f}{\partial y \partial x}(0,0) = \lim_{t \rightarrow 0} \frac{\frac{\partial f}{\partial x}(0,t) - \frac{\partial f}{\partial x}(0,0)}{t} = \lim_{t \rightarrow 0} \frac{t \frac{-t^2}{t^2 + 0} + 0 - 0}{t} = -1$$

$$\frac{t \frac{-t^2}{t^2} + 0 - 0}{t} = -1$$

$$f(x_1, x_2) = x_1^3 + x_2^2$$

$$\Delta f = \frac{\partial^2}{\partial x_1^2} f + \frac{\partial^2}{\partial x_2^2} f = 6x_1 + 2$$

$$L = f(x, z) = \begin{pmatrix} f_1(x, z) \\ f_2(x, z) \end{pmatrix}$$

$$m = 2$$

$$n = 3$$

$$\left(\frac{\partial f_1}{\partial x_1}, \frac{\partial f_1}{\partial x_2}, \frac{\partial f_1}{\partial z} \right)^T = \nabla f_1$$

$$\frac{\partial f}{\partial x} = \begin{pmatrix} \frac{\partial f_1}{\partial x_1} \\ \frac{\partial f_1}{\partial x_2} \end{pmatrix}$$

$$f(x_1, x_2) = x_1^2 + x_2^2$$

