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Open Reading for Free Choice Permission

A Perspective from Substructural Logics

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- Motivations
- Open Reading
- Substructural Logics
- An Example
- Conclusions

■ Standard Deontic Logic: Permission =_{df} the dual of Obligation

- $O(A \wedge B) \subset \supset OA \wedge OB$

- $P(A \vee B) \subset \supset PA \vee PB$

■ Many faces of permissions:

strong/weak permission, explicit/implicit/tacit permission, free choice permission (FCP), open reading, etc.

■ Dynamic approach of free choice permission:

$$P(A) = [A] \neg \text{Violation}$$

■ Canonical Form of FCP:

$$P(A \vee B) \supset PA \wedge PB$$

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1 $PA \supset P(A \wedge B)$

- Monotonic case: Vegetarian free lunch

$$P(\text{Order}) \supset P(\text{Order} \wedge \text{not Pay})$$

- Resource insensitive case:

$$P(\text{Eat a cookie}) \supset P(\text{Eat a cookie} \wedge \text{Eat a cookie})$$

2 $P(A \vee \sim A) \supset PB$

- Irrelevant case:

$$P(\text{Open Window} \vee \text{not Open Window}) \subset \supset P(\text{Sell House} \vee \text{not Sell House}) \\ \supset P(\text{Sell House})$$

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Resource Sensitivity

Chris Barker. *Free choice permission as resource-sensitive reasoning*. Semantics and Pragmatics, 2010.

Negation

Sun Xin and H. Dong. *The deontic dilemma of action negation, and its solution*. LOFT 2014.

Three Difficulties in FCP

Albert J.J. Anglberger, H. Dong, and Olivier Roy. *Open reading without free choice*. DEON 2014.

and so on...

1 Open Reading (OR):

An action type A is permitted iff each token of A is normatively OK.

2 FCP inference

$$A \multimap B \vdash PB \supset PA$$

3 Our two-fold strategy:

1 To avoid the problems: $(A \wedge B) \multimap A$, $(A \wedge \dots \wedge A) \multimap A$, and $(A \vee \sim A) \multimap (B \vee \sim B)$

2 To save the plausible case:

$$(Order \wedge Pay) \multimap Order \vdash P(Order) \supset P(Order \wedge Pay)$$

4 $A \multimap B$: “If A , normally, then B .”

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Why Substructural Logic?

To achieve a systematic view of semantic variety in the landscape of logics for FCP.

Definition (Formulas)

The set \mathcal{L} of well-formed formulas of normality is defined as follows:

$$A := p \mid \perp \mid \neg A \mid (A \uplus A) \mid (A \circ A) \mid (A \multimap A) \mid P(A)$$

where $p \in Act_0$ where Act_0 is the set of all atomic propositions with regards to actions.

$$A \supset B =_{def} \neg A \uplus B.$$

- How to understand $A \circ B$:
 - “doing A together with doing B ”
 - concurrent action:
Listen \circ *Write Note*
- How to understand $A \rightarrow B$:
 - “doing A counting as doing B ”
 - count-as relations:
Cycle \rightarrow *Travel By Vehicle*,
Order Lunch \rightarrow *Pay*

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Cycle \rightarrow *Travel By Vehicle*,
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Definition (Structures)

The set \mathcal{S} of structures of normality is defined as follows:

$$X := A \mid 1 \mid (X; X) \mid (X, X).$$

where $A \in \mathcal{L}$ is a well-formed formula.

$X[Y]$ means a structure X with a substructure Y , while $X[Z/Y]$ means a structure X with replacing the occurrences of the substructure Y by Z .

A frame for normality is a tuple $\mathcal{F} = \langle W, M, OK \rangle$ where

- W is a non-empty set of events
- $M \subseteq W \times W \times W$ is a ternary relation on W
- $OK \subseteq W \times W$ is a binary relation on W

Possible readings:

- 1 $Mwyz$:
An event w combining/composing with an event y leads to an event z .
- 2 $OK(y, w)$:
Seeing from event w , y is normatively OK.

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Models

Let a tuple $\mathcal{M} = \langle \mathcal{F}, V \rangle$ be a model based on a frame \mathcal{F} for normality, a function $V : Act_0 \rightarrow \wp(W)$ assigning a set of events such that $V(p) \subseteq W$ for all $p \in Act_0$, where $p \in Act_0$. A well-formed formula $A \in \mathcal{L}$ is *true* at event w in model \mathcal{M} , written $\mathcal{M}, w \models A$, and a structure X is true at w in \mathcal{M} , written $\mathcal{M}, w \models X$, are defined as follows:

$\mathcal{M}, w \models p$	iff	$w \in V(p)$
$\mathcal{M}, w \not\models \perp$		for all $w \in W$
$\mathcal{M}, w \models \neg A$	iff	$\mathcal{M}, w \not\models A$
$\mathcal{M}, w \models A \uplus B$	iff	$\mathcal{M}, w \models A$ or $\mathcal{M}, w \models B$
$\mathcal{M}, w \models A \multimap B$	iff	$\forall y, z \in W. (\mathcal{M}, y \models A \ \& \ Mwyz \Rightarrow \mathcal{M}, z \models B)$
$\mathcal{M}, w \models A \circ B$	iff	$\exists y, z \in W. (\mathcal{M}, y \models A, \mathcal{M}, z \models B \ \& \ Myzw)$
$\mathcal{M}, w \models PA$	iff	$\forall y, z \in W. (\mathcal{M}, y \models A \Rightarrow OK(y, w))$
$\mathcal{M}, w \models 1$		for each $w \in W$
$\mathcal{M}, w \models X; Y$	iff	$\exists y, z \in W. (\mathcal{M}, y \models X, \mathcal{M}, z \models Y \ \& \ Myzw)$
$\mathcal{M}, w \models X, Y$	iff	$\mathcal{M}, w \models X$ and $\mathcal{M}, w \models Y$

A basic sequent calculus N^0 of normality:

$$(\circ R) \frac{X \vdash A \quad Y \vdash B}{X; Y \vdash A \circ B}$$

$$(\circ L) \frac{X[A; B] \vdash C}{X[A \circ B] \vdash C}$$

$$(\rightarrow R) \frac{X; A \vdash B}{X \vdash A \rightarrow B}$$

$$(\rightarrow L) \frac{X \vdash A \quad Y[B] \vdash C}{Y[A \rightarrow B; X] \vdash C}$$

$$(Id) \quad p \vdash p \text{ where } p \in Act_0$$

$$(Cut) \frac{X \vdash A \quad Y[A] \vdash B}{Y[X/A] \vdash B}$$

$$(Tra) \frac{X; A \vdash B \quad Y; B \vdash C}{(X, Y); A \vdash C}$$

$$(OR) \frac{X; A \vdash B}{X, P(B) \vdash P(A)}$$

One Extension N^{RaM}

$$(RaM) \frac{X \vdash A \multimap C}{X \vdash \neg((A \circ B) \multimap \perp) \supset (A \circ B) \multimap C}$$

- Normality: $\forall w \forall x \forall y' [\forall y (Mwy'y \supset OK(y, x)) \supset OK(y', x)]$.

$$(OR) \frac{X; A \vdash B}{X, P(B) \vdash P(A)}$$

- Transitivity of Normality: $\forall x \forall y \forall z \exists u [Mxyz \supset Mxyu \wedge Mxuz]$.

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- Rational Monotonicity:

$$\forall x \forall y \forall z \forall s \forall u \forall y' \forall z' \forall s' \forall u' [(Mxyz \wedge Msuy) \wedge (Mxy'z' \wedge Mz's'u') \supset (Mxsz \vee Mxy'z')]$$

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An acceptable rational monotonic case:

- (1) $Order \multimap Order \vdash Order \multimap Order$ (Id)
- (2) $Order \multimap Order \vdash \neg(Order \circ Pay \multimap \perp) \supset (Order \circ Pay) \multimap Order$ (1), (RaM)
- (3) $Order \multimap Order, \neg(Order \circ Pay \multimap \perp) \vdash P(Order) \supset P(Order \circ Pay)$ (2), (OR)

where $Order, Pay \in Act_0$.

- 1 The logics N^0 and N^{RaM} can avoid the undesired FCP results. In addition, N^{RaM} can implies the desired FCP by applying (RaM).
- 2 Define obligation in this substructural framework, and check the interaction of obligation and permission.
- 3 Compare this ternary framework with the binary framework proposed by van Benthem (1979).

Thank you!