Nilmanifolds: a nearly linear playground for geometric structures

Nilmanifolds, that is, compact quotients of nilpotent Lie-groups, have over the last decades furnished many examples of exotic geometric structures. I will try to indicate how many geometric problems on nilmanifolds can be translated into linear algebra (and then maybe solved) and illustrate the procedure with some examples related to complex geometry.