Infinite transitivity of automorphism groups

Abstract:

Given an affine algebraic variety X of dimension at least 2, we let SAut(X) denote its special automorphism group of i.e. the subgroup of the full automorphism group Aut(X) generated by all one-parameter unipotent subgroups. We show that if SAut(X) acts transitively on the smooth locus Reg(X) then it is infinitely transitive on Reg(X). In turn, the transitivity is equivalent to the flexibility of X. The latter means that for every smooth point of X the tangent space is spanned by the velocity vectors of one-parameter unipotent subgroups of Aut(X). We provide also different variations and applications.