

Figure 1: A ("globular") 3-morphism in an  $\omega$ -category. The 3-morphism  $V: \Sigma_1 \Rightarrow \Sigma_2$  goes between the 2-morphisms  $\Sigma_1, \Sigma_2: \gamma_1 \to \gamma_2$  which in turn have as source the object x and as target the object y.

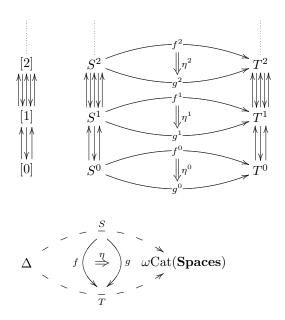


Figure 2: Higher morphisms between cosimplicial  $\omega$ -categories. Here  $S,T:\Delta\to\omega\mathrm{Cat}(\mathbf{Spaces})$  are two cosimplicial  $\omega$ -categories internal to  $\mathbf{Spaces},\ f,g:S\to T$  are two 1-morphisms between them and  $\eta:f\Rightarrow G$  a 2-morphism between these. The upper diagram shows the component  $\omega$ -functors and their naturality condition. All parallel diagrams on the right strictly commute.

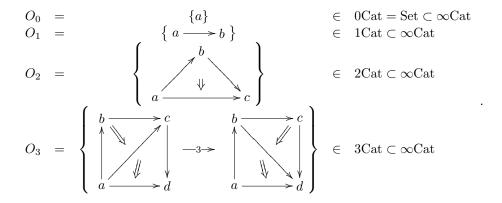


Figure 3: **Orientals.** The *n*-th oriental  $O_n \in n$ Cat  $\subset \omega$ Cat is the free *n*-category on a single *n*-simplex. The first 4 orientals are shown explicitly. Here  $O_3$  is to be thought of as a tetrahedron, filled by the 3-morphism  $\xrightarrow{3}$ , which we have depicted after slicing it open.

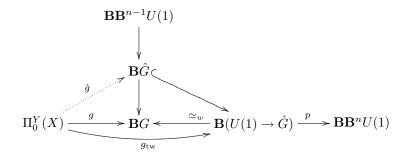


Figure 4: **Obstruction theory** for lifts of nonabelian cocycles through shifted central extensions  $\mathbf{B}^{n-1}U(1) \to \hat{G} \to G$ . The lift  $\hat{g}$  of the G-cocycle g is obstructed by the  $\mathbf{B}^nU(1)$ -cocycle  $p \circ g_{\mathrm{tw}}$ , where  $g_{\mathrm{tw}}$  is a twisted  $\hat{G}$ -cocycle, namely a  $\hat{G}//\mathbf{B}^{n-1}U(1)$ -cocycle a lift to which always exists for sufficiently fine cover Y.

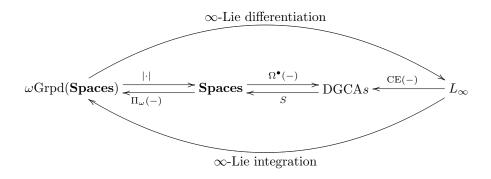


Figure 5: The basic structure of  $\infty$ -Lie theory as conceived here.

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