

MR0293130 (45 #2209) 32F10

Riemenschneider, Oswald

Halbstetigkeitssätze für 1-konvexe holomorphe Abbildungen. (German)

*Math. Ann.* **192** (1971), 216–226.

Suppose that  $f: X \rightarrow Y$  is a  $p$ -convex holomorphic map and  $S$  is an  $f$ -flat coherent analytic sheaf on  $X$ . For  $y \in Y$  let  $X_y$  be the fiber of  $X$  above  $y$  and let  $S_y$  be the analytic restriction of  $S$  to  $X_y$ . Define  $d_q(y) = \dim H^q(X_y, S_y)$ . The author proves the following: (I) For  $q \geq p$ ,  $d_q$  is upper semi-continuous on  $Y$  and, when  $Y$  is reduced, is locally constant outside a lower-dimensional analytic subset of  $Y$ . (II) If  $Y$  is reduced and  $d_q$  is locally constant for some  $q \geq p$ , then the  $q$ th direct image of  $S$  is locally free. The proof rests on the author's method for the proper case [same *Ann.* **187** (1970), 40–55; MR0261039] together with the blow-down of 1-convex maps. For related results, compare with the reviewer's paper [ibid. **190** (1970/71), 203–214; MR0279341].

Y.-T. Siu

© Copyright American Mathematical Society 1973, 2016