Reasoning and Formal Modelling for Forensic Science Lecture 5

Prof. Dr. Benedikt Löwe

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Prof. Dr. Benedikt Löwe

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# Reminder: Controlled Situations.

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## Reminder: Controlled Situations.

Every A is B. Some C is B.

Some C is A.

**Example.** *A*: "Dutch citizen", *B* "citizen of an EU country", *C* "Bulgarian citizen". Fix five people in a room: *a*, *b*, *c*, *d*, *e*.

*a* is a Bulgarian citizen, *b* is a US citizen, *c*, *d*, and *e* are Dutch citizens. All Dutch and Bulgarian citizens are EU citizens (and only those). None of the five people has a dual nationality.

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*a* is a Bulgarian citizen, *b* is a US citizen, *c*, *d*, and *e* are Dutch citizens. All Dutch and Bulgarian citizens are EU citizens (and only those). None of the five people has a dual nationality.

Then this controlled situation makes "Every A is B" and "Some C is B" true, but not "Some C is A", and this shows the invalidity of the above syllogism.

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A controlled situation consists of a collection of individuals. These are often human beings, but can also be items or abstract entities. Reasoning and Formal Modelling for Forensic Science Lecture 5

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In addition, we have some properties. For each individual e and each property P, it can either be that e has property P or not. We need to give complete descriptions of all of these cases.

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In the case of controlled situations for syllogisms, we have three properties: A, B, and C. Reasoning and Formal Modelling for Forensic Science Lecture 5

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- If there are only finitely many individuals and finitely many properties, then this can easily be written in a matrix:

	P	Q	R	5
$e_0$	Yes	No	Yes	No
$e_1$	Yes	Yes	Yes	No
$e_2$	Yes	No	No	Yes

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- If there are only finitely many individuals and finitely many properties, then this can easily be written in a matrix:

	P	Q	R	S
$e_0$	Yes	No	Yes	No
$e_1$	Yes	Yes	Yes	No
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In order to abbreviate statements like "e has property P", we typically write P(e).

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### Reminder: Proving that a mood is invalid.

**Algorithm.** Suppose you have an Aristotelian mood that you want to show invalid. The mood involves the terms A, B and C and has two premisses  $\varphi$  and  $\psi$  and a conclusion  $\chi$ .

*Step 1.* Draw the Venn diagram for the mood. This gives you an indication how to invalidate the mood.

Step 2. Describe a controlled situation by giving individuals with well-defined properties A, B, and C.

Step 3. Argue that each of the premisses  $\varphi$  and  $\psi$  is true in the controlled situation.

Step 4. Argue that the conclusion  $\chi$  is not true in the controlled situation.

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There is an A that is B. Some B is not C.

No A is C.

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There is an A that is B. Some B is not C.

No A is C.

Step 2. Take two individuals: g (gun) and k (knife).

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A: murder weapon, B: has fingerprints of the suspect, C: has blood of the victim.

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Step 2. Take two individuals: g (gun) and k (knife).

A: murder weapon, B: has fingerprints of the suspect, C: has blood of the victim.

The knife is the murder weapon, has blood of the victim, and has fingerprints. The gun is not the murder weapon, has no blood, but has fingerprints of the suspect: Reasoning and Formal Modelling for Forensic Science Lecture 5

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A: murder weapon, B: has fingerprints of the suspect, C: has blood of the victim.

The knife is the murder weapon, has blood of the victim, and has fingerprints. The gun is not the murder weapon, has no blood, but has fingerprints of the suspect:

	Α	В	С
g	No	Yes	No
k	Yes	Yes	Yes

Step 3. k is both A and B; g is B but not C.

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No A is C.

Step 2. Take two individuals: g (gun) and k (knife).

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The knife is the murder weapon, has blood of the victim, and has fingerprints. The gun is not the murder weapon, has no blood, but has fingerprints of the suspect:

	Α	В	С
g	No	Yes	No
k	Yes	Yes	Yes

Step 3. k is both A and B; g is B but not C. Step 4. k is both A and C. Reasoning and Formal Modelling for Forensic Science Lecture 5

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Aristotelean Syllogistics is a very restricted setting: we have exactly three properties A, B and C, and all sentences are of one of the four forms

"All X are Y" "Some X are Y" "No X are Y" "Some X are not Y" Reasoning and Formal Modelling for Forensic Science Lecture 5

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In controlled situations, we can evaluate many more sentences:

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In controlled situations, we can evaluate many more sentences:

- Simpler sentences like "Everything is X", "Something is X".
- More complex sentences like "All X are Y, and not all Y are X."

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In controlled situations, we can evaluate many more sentences:

- Simpler sentences like "Everything is X", "Something is X".
- More complex sentences like "All X are Y, and not all Y are X."

In other words, we can use our binary and unary connectives to link sentences together:  $\land$ ,  $\lor$ ,  $\neg$ ,  $\rightarrow$ .

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The syllogism itself can be seen as such a combination: if  $\varphi$  and  $\psi$  are the premisses and  $\chi$  is the conclusion, then the syllogism is  $\varphi \wedge \psi \rightarrow \chi$ .

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**Observation.** Our algorithm for checking whether a mood with premisses  $\varphi$  and  $\psi$  and conclusion  $\chi$  is invalid shows that the formula  $\varphi \land \psi \rightarrow \chi$  is invalid by the method of truth tables.

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$\varphi$	T	Т	Т	Т	F	F	F	F
$\dot{\psi}$	Т	Т	F	F	Т	Т	F	F
$\chi$	Т	F	Т	F	Т	F	Т	F

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$\varphi$	T	т	Т	Т	F	F	F	F
$\dot{\psi}$	Т	т	F	F	Т	Т	F	F
$\chi$	Т	F	Т	F	Т	F	Т	F
$\varphi \wedge \psi$	Т	Т	F	F	F	F	F	F
$(\varphi \wedge \psi) \rightarrow \chi$	Т	F	Т	Т	Т	Т	т	Т
		↑						

There is exactly one combination of truth values that invalidates a mood, and the algorithm asks us to produce a controlled situation for that combination of truth values. Reasoning and Formal Modelling for Forensic Science Lecture 5

### A special case: finite controlled situations

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A controlled situation is called finite if there are finitely many individuals. Otherwise it is called infinite.

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A controlled situation is called finite if there are finitely many individuals. Otherwise it is called infinite.

In finite controlled situations, the quantifiers "for all", "some", "no" and "some — not" can be represented by the binary and unary connectives.

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Consider the controlled situation with the individuals j (John), s (Sue), and b (Bill), and properties H (human), M (male), and F (female). We give the values of the properties in a table:

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	H	М	F
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5	Yes	No	Yes
b	Yes	Yes	No

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In this situation, the statement "All males are human" (All M are H) is true.

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In this situation, the statement "All males are human" (All M are H) is true. But in this situation, we can express it by the following formula that does not involve quantifiers:

$$(H(j) \rightarrow M(j)) \land (H(s) \rightarrow M(s)) \land (H(b) \rightarrow M(b)).$$

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This is not the case in general in infinite controlled situations:

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This is not the case in general in infinite controlled situations:

Consider the natural numbers  $\mathbb{N}=\{0,1,2,3,...\}$  as our individuals and use the three properties

BiggerThanTwo →  $\{3, 4, 5, 6, 7, ...\},$ Odd →  $\{1, 3, 5, 7, 9, ...\},$ Prime →  $\{2, 3, 5, 7, 11, 13, ...\}.$ 

(A number is prime if it is not divisible by a smaller number other than 1.)

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 $\forall x (BiggerThanTwo(x) \land Prime(x) \rightarrow Odd(x)).$ 

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(A number is prime if it is not divisible by a smaller number other than 1.)

"If x > 2 and x is prime, then x is odd."

 $\forall x (BiggerThanTwo(x) \land Prime(x) \rightarrow Odd(x)).$ 

But this cannot be expressed by connectives, as you will never be able to finish the formula describing it (as  $\mathbb{N}$  is infinite).

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We now introduce symbols for the quantifiers:

 $\begin{array}{cc} \text{``AII''} & \text{``Some''} \\ \forall & \exists \end{array}$ 

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"All" "Some" ∀ ∃

 $\forall$  is called the universal quantifier and  $\exists$  is called the existential quantifier.

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 $\forall$  is called the universal quantifier and  $\exists$  is called the existential quantifier. We write

 $\forall x P(x)$ 

for "all individuals have property P" and  $\exists x P(x)$ 

for "some individual has property P".

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 $\forall$  is called the universal quantifier and  $\exists$  is called the existential quantifier. We write

 $\forall x P(x)$ 

for "all individuals have property P" and

 $\exists x P(x)$ 

for "some individual has property P". Note that we do not need symbols for "no" and "some — not", as they can be defined from  $\forall$  and  $\exists$ :

"No individuals have property P" "Some individuals don't have property P"  $\forall x \neg P(x) \qquad \exists x \neg P(x)$  Reasoning and Formal Modelling for Forensic Science Lecture 5

Reasoning and Formal Modelling for Forensic Science Lecture 5

We fix a controlled situation S with a collection E of individuals and some properties  $P_0, ..., P_n$ . We say

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 $P_i(e)$  is valid in S if and only if e has property  $P_i$ 

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We fix a controlled situation S with a collection E of individuals and some properties  $P_0, ..., P_n$ . We say

$P_i(e)$ is valid in S	if and only if $e$ has property $P_i$
$arphi \wedge \psi$ is valid in $S$	if and only if $arphi$ is valid in ${\it S}$
	and $\psi$ is valid in ${\it S}$

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We fix a controlled situation S with a collection E of individuals and some properties  $P_0, ..., P_n$ . We say

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$arphi\wedge\psi$ is valid in $S$	if and only if $arphi$ is valid in ${\it S}$
	and $\psi$ is valid in $S$
$\varphi \lor \psi$ is valid in $S$	if and only if $arphi$ is valid in $S$
	or $\psi$ is valid in S

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eg arphi is valid in $S$	if and only if $\varphi$ is not valid in $S$

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$\varphi \lor \psi$ is valid in $S$	if and only if $arphi$ is valid in ${\it S}$
	or $\psi$ is valid in ${\cal S}$
eg arphi is valid in $S$	if and only if $arphi$ is not valid in ${\it S}$
$\forall x \varphi$ is valid in S	if and only if no matter which $e \in E$ we
	choose, if we replace all occurrances of $x$
	in $\varphi$ by e, then this formula $\varphi \frac{e}{x}$ is valid.

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We fix a controlled situation S with a collection E of individuals and some properties  $P_0, ..., P_n$ . We say

$P_i(e)$ is valid in S	if and only if $e$ has property $P_i$
$arphi\wedge\psi$ is valid in $S$	if and only if $arphi$ is valid in ${\it S}$
	and $\psi$ is valid in ${\it S}$
$\varphi \lor \psi$ is valid in $S$	if and only if $arphi$ is valid in $S$
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$\forall x \varphi$ is valid in $S$	if and only if no matter which $e \in E$ we
	choose, if we replace all occurrances of $x$
	in $\varphi$ by $e$ , then this formula $\varphi \frac{e}{x}$ is valid.
$\exists x \varphi$ is valid in S	if and only there is some $e \in \vec{E}$ such that if
	we replace all occurrances of $x$ in $\varphi$
	by <i>e</i> , then this formula $\varphi \frac{e}{x}$ is valid.

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We have three individuals, s (Socrates), p (Plato), and a (Aristotle), and three properties T (teacher), S student, and P (philosopher).

	T	5	Р	
5	Yes	No	Yes	
р	Yes	Yes	Yes	
а	No	Yes	Yes	

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Every teacher is a philosopher.

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	Т	S	Р
5	Yes	No	Yes
р	Yes	Yes	Yes
а	No	Yes	Yes

• Every teacher is a philosopher.  $\forall x(T(x) \rightarrow P(x))$  Reasoning and Formal Modelling for Forensic Science Lecture 5

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	T	5	Р
5	Yes	No	Yes
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► Every teacher is a philosopher.  

$$\forall x(T(x) \rightarrow P(x))$$
  
 $(T(s) \rightarrow P(s)) \land (T(p) \rightarrow P(p)) \land (T(a) \rightarrow P(a))$ 

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• Every teacher is a philosopher.  

$$\forall x(T(x) \rightarrow P(x))$$
  
 $(T(s) \rightarrow P(s)) \land (T(p) \rightarrow P(p)) \land (T(a) \rightarrow P(a))$   
 $\rightsquigarrow$  YES!

Reasoning and Formal Modelling for Forensic Science Lecture 5

We have three individuals, s (Socrates), p (Plato), and a (Aristotle), and three properties T (teacher), S student, and P (philosopher).

	T	S	Р
5	Yes	No	Yes
р	Yes	Yes	Yes
а	No	Yes	Yes

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 $\rightarrow No!$ 

Reasoning and Formal Modelling for Forensic Science Lecture 5

Reasoning and Formal Modelling for Forensic Science Lecture 5

#### Police report, Colorado Springs, 17 Feb 2011, 3:40 am:

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Individuals: m (male), o (officers). Properties: D (took drugs), S (has unusual strength), A (is arrested).

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Reasoning and Formal Modelling for Forensic Science Lecture 5

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There is someone who has unusual strength who didn't get arrested.

Reasoning and Formal Modelling for Forensic Science Lecture 5

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	D	S	Α
т	Yes	Yes	Yes
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- Everyone who took drugs has unusual strength.  $\forall x(D(x) \rightarrow S(x))$   $(D(m) \rightarrow S(m)) \land (D(o) \rightarrow S(o))$  $\rightsquigarrow$  YES!
- ► There is someone who has unusual strength who didn't get arrested.  $\exists x(S(x) \land \neg A(x))$

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There is someone who has unusual strength who didn't get arrested. ∃x(S(x) ∧ ¬A(x)) (S(m) ∧ ¬A(m)) ∨ (S(o) ∧ ¬A(o)) Reasoning and Formal Modelling for Forensic Science Lecture 5

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► There is someone who has unusual strength who didn't get arrested.  $\exists x(S(x) \land \neg A(x))$   $(S(m) \land \neg A(m)) \lor (S(o) \land \neg A(o))$  $\Rightarrow$  No! Reasoning and Formal Modelling for Forensic Science Lecture 5

Reasoning and Formal Modelling for Forensic Science Lecture 5

Police report, Colorado Springs, 16 Feb 2011, 7:54 am:

Officers responded in regards to an unresponsive female found inside of the home. When officers arrived they contacted members of the Colorado Springs Fire Department who indicated that the female was deceased. A short time later, the 20 year old female was pronounced dead by medical personnel. At this time, there are no identifiable suspicious circumstances surrounding the death. However, the exact cause of death has not been determined. The El Paso County Coroners Office responded and took possession of the female. They will be performing an autopsy in an attempt to determine a cause of death. Reasoning and Formal Modelling for Forensic Science Lecture 5

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Individuals: f (female), m (medical personnel). Properties: U (unresponsive), D (dead), P (makes a pronouncement of death).

	U	D	Р
f	Yes	Yes	No
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There is someone who is neither dead nor pronounced someone dead.

Reasoning and Formal Modelling for Forensic Science Lecture 5

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Reasoning and Formal Modelling for Forensic Science Lecture 5

We didn't express "the medical personnel pronounced the female dead", but only "the medical personnel pronounced someone dead and the female is dead".

Reasoning and Formal Modelling for Forensic Science Lecture 5

We didn't express "the medical personnel pronounced the female dead", but only "the medical personnel pronounced someone dead and the female is dead". Is that the same?

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**No:** In a controlled situation with two dead people, it could be that the medical personnel only pronounced one of them dead.

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Formally: a controlled situation with individuals f (female), d (dog), m (medical personnel) and properties D (dead) and P (made a pronouncement of death).

	D	Ρ
f	Yes	No
d	Yes	No
т	No	Yes

Reasoning and Formal Modelling for Forensic Science Lecture 5

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Formally: a controlled situation with individuals f (female), d (dog), m (medical personnel) and properties D (dead) and P (made a pronouncement of death).

	D	Р
f	Yes	No
d	Yes	No
т	No	Yes

How do we express that the medical personnel only pronounced the female dead, but not the dog?

Reasoning and Formal Modelling for Forensic Science Lecture 5

Reasoning and Formal Modelling for Forensic Science Lecture 5

Leibniz's Monadology: attempt to reduce everything to properties

Reasoning and Formal Modelling for Forensic Science Lecture 5

Leibniz's Monadology: attempt to reduce everything to properties

Bertrand Russell, A Critical Exposition of the Philosophy of Leibniz. Cambridge University Press, 1900.

The question whether all propositions are reducible to subject-predicate form is one of fundamental importance to all philosophy. ... I cannot here, however, do more than indicate the grounds for rejecting the traditional view. ... We must admit, ... relations between subjects [cannot be regarded as a mere sum of subject-predicate propositions]—e.g. relations of position, of greater and less, of whole and part. (pp. 13–14) Reasoning and Formal Modelling for Forensic Science Lecture 5

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Examples.

Reasoning and Formal Modelling for Forensic Science Lecture 5

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#### Examples.

The medical personnel pronounces the female dead.

Reasoning and Formal Modelling for Forensic Science Lecture 5
# Is MQL enough? (2)

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#### Examples.

- The medical personnel pronounces the female dead.
- Jeff kills Sue.

Reasoning and Formal Modelling for Forensic Science Lecture 5

# Is MQL enough? (2)

Leibniz's Monadology: attempt to reduce everything to properties

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#### Examples.

- The medical personnel pronounces the female dead.
- Jeff kills Sue.
- Plato is the teacher of Socrates.

Reasoning and Formal Modelling for Forensic Science Lecture 5

A controlled situation with relations is a controlled situation together with some relations  $R_0, ..., R_m$ . We fix a controlled situation with relations S: collection E of individuals, some properties  $P_0, ..., P_n$  and some relations  $R_0, ..., R_m$ . We say Reasoning and Formal Modelling for Forensic Science Lecture 5

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 $P_i(e)$  is valid in S if and only if e has property  $P_i$  $R_j(e, f)$  is valid in S if and only if e and f are in relation  $R_j$  Reasoning and Formal Modelling for Forensic Science Lecture 5

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Reasoning and Formal Modelling for Forensic Science Lecture 5

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A female victim called 911 to report that she had been stabbed near the Stargazers Theater ... The victim reported a Hispanic male in his late 20's to early 30's attempted to rob her, and he stabbed her in the stomach area. Officers and medical personnel contacted the victim in the south parking lot of the Stargazers Theatre and she was transported to the hospital to have the knife removed from her lower stomach area. The victim described the suspect as a Hispanic male in his late 20's to early 30's, approximately 5-10 in height with a heavier build and a ponytail. The suspect was reported to be wearing a plain black long sleeve shirt, jeans, and black gloves. Officers searched the area but were unable to locate the suspect. Reasoning and Formal Modelling for Forensic Science Lecture 5

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Individuals: f (female), m (male), o (officers). Properties: H (hospitalized). Relations: S (stabbed), L (located).

	H	S	f	т	0		L	f	т	0
f	Yes	f	No	No	No	-	f	No	No	No
т	No	т	Yes	No	No		т	No	No	No
0	No	0	No	No	No		0	Yes	No	No

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	H	S	f	т	0		L	f	т	0
f	Yes	f	No	No	No	-	f	No	No	No
т	No	m	Yes	No	No		m	No	No	No
0	No	0	No	No	No		0	Yes	No	No

Someone who stabbed someone else is still not located.

Reasoning and Formal Modelling for Forensic Science Lecture 5

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	H	S	f	т	0		L	f	т	0
f	Yes	f	No	No	No	-	f	No	No	No
т	No	т	Yes	No	No		т	No	No	No
0	No	0	No	No	No		0	Yes	No	No

Someone who stabbed someone else is still not located.  $\exists x (\exists y S(x, y) \land \forall z \neg L(z, x))$  Reasoning and Formal Modelling for Forensic Science Lecture 5

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	H	S	f	т	0		L	f	т	0
f	Yes	f	No	No	No	-	f	No	No	No
т	No	т	Yes	No	No		т	No	No	No
0	No	0	No	No	No		0	Yes	No	No

Someone who stabbed someone else is still not located.  $\exists x (\exists y S(x, y) \land \forall z \neg L(z, x))$  $S(m, f) \land (\neg L(f, m) \land \neg L(m, m) \land \neg L(o, m))$  Reasoning and Formal Modelling for Forensic Science Lecture 5

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	H	S	f	т	0	L	f	т	0
f	Yes	f	No	No	No	f	No	No	No
т	No	т	Yes	No	No	m	No	No	No
0	No	0	No	No	No	0	Yes	No	No

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т	No	т	Yes	No	No	т	No	No	No
0	No	0	No	No	No	0	Yes	No	No

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There is someone who got stabbed but was not hospitalized.

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	H	S	f	т	0	L	f	т	0
f	Yes	f	No	No	No	f	No	No	No
т	No	т	Yes	No	No	т	No	No	No
0	No	0	No	No	No	0	Yes	No	No

Someone who stabbed someone else is still not located.  $\exists x (\exists y S(x, y) \land \forall z \neg L(z, x))$   $S(m, f) \land (\neg L(f, m) \land \neg L(m, m) \land \neg L(o, m))$   $\rightsquigarrow YES!$ 

► There is someone who got stabbed but was not hospitalized.  $\exists x (\exists y S(y, x) \land \neg H(x))$  Reasoning and Formal Modelling for Forensic Science Lecture 5

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	H	S	f	т	0	L	f	т	0
f	Yes	f	No	No	No	f	No	No	No
т	No	т	Yes	No	No	т	No	No	No
0	No	0	No	No	No	0	Yes	No	No

Someone who stabbed someone else is still not located.  $\exists x (\exists y S(x, y) \land \forall z \neg L(z, x))$   $S(m, f) \land (\neg L(f, m) \land \neg L(m, m) \land \neg L(o, m))$   $\rightsquigarrow YES!$ 

There is someone who got stabbed but was not hospitalized. ∃x(∃yS(y, x) ∧ ¬H(x)) S(m, f) ∧ H(f), ¬∃yS(y, m), ¬∃yS(y, o) Reasoning and Formal Modelling for Forensic Science Lecture 5

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	H	S	f	т	0	L	f	т	0
f	Yes	f	No	No	No	f	No	No	No
т	No	т	Yes	No	No	т	No	No	No
0	No	0	No	No	No	0	Yes	No	No

Someone who stabbed someone else is still not located.  $\exists x (\exists y S(x, y) \land \forall z \neg L(z, x))$   $S(m, f) \land (\neg L(f, m) \land \neg L(m, m) \land \neg L(o, m))$  $\rightsquigarrow$  **YES!** 

► There is someone who got stabbed but was not hospitalized.  $\exists x (\exists y S(y, x) \land \neg H(x))$   $S(m, f) \land H(f), \neg \exists y S(y, m), \neg \exists y S(y, o)$  $\Rightarrow$  No! Reasoning and Formal Modelling for Forensic Science Lecture 5